An Extension to Pointer Logic for Verification

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Abstract

The safety of pointer programs is an important issue in high-assurance software design, and their verification remains a major challenge. Pointer Logic has been proposed to verify basic safety properties of pointer programs in our previous work, but still lacks support for a wide range of pointer programs. In this work, we present an extension to Pointer Logic by: 1) introducing modular reasoning to scale better on programs involving function calls; 2) allowing pointer arithmetic to take more advantage of pointers in programming. Moreover, to demonstrate that Pointer Logic is a useful approach to verification, we implement a tool – \textsc{plcc} to automatically verify a range of non-trivial programs, including basic operations on singly-linked lists, trees, circular doubly-linked list, dynamic arrays etc..

1. Introduction

Nowadays software is widely used in various areas, and potential errors such as dangling dereferences and memory leaks might lead to serious damages. As a result, high-assurance software is highly desirable. On the other hand, software verification promises to overcome the current software crisis of bug-ridden software. Pointers (references) are widely used in modern programming languages for its efficiency and flexibility, but they are also the source of errors because of aliasing.

In recent years, program verification through formal reasoning to predict the effect that a program produces when run on a physical machine, has made great progress in software engineering. PCC (Proof Carrying Code) [16] pioneered by Necula has given light into the verification paradigm which can be applied in actual software development. In order to utilize the PCC paradigm for verification, various approaches e.g., [15, 1, 23, 22] are proposed. However, many of these approaches based on formal reasoning need a theory to describe the semantics of the programming language, and introduce concepts such as heaps, stacks \textit{etc.} explicitly that are not part of the syntax. Although useful in reasoning about program properties, they complicate the reasoning significantly. On the contrary, Pointer Logic explores the possibility to directly handle the program safety properties of a given state through sets of access paths (pointers) instead of introducing stacks or heaps explicitly – the reasoning is all syntactic.

Pointer Logic has been reported on in two earlier works [6, 7]. However, existing Pointer Logic rules for function calls associate the entire heap with each invocation, and the function body might be verified more than once, thus it is difficult to scale the current approach to more programs. We believe that modular treatment of the heap will allow the implementation to scale better on larger pieces of code. Moreover, it lacks support for pointer arithmetic, which hinders wide usage of Pointer Logic for program verification. In this work, we take a leap forward in addressing the aforementioned issues by introducing modular reasoning and extending Pointer Logic with pointer arithmetic. We consider the case of a C-like imperative language–\textsc{PointerC}, which includes pointer arithmetic but excludes the address-of operation. Although in [6, 7] a previous version of \textsc{plcc}(v1.5) was released, it can only verify several simple programs and verification conditions generated need proving manually in COQ [8]. Therefore, we redesigned \textsc{plcc}(Current version is v2.0) to verify a range of pointer programs without any help from interactive theorem provers – it’s fully automated. As long as the programs are annotated with loop invariants, pre- and post-conditions, the annotations are then automatically checked for validity by calculating the strongest post-conditions according to Pointer Logic rules and verifying a number of induced implications internally.

Our contributions can be summarized as follows:

1. We introduce modular reasoning in Pointer Logic by splitting the program states via reachability of objects,
which enables us to verify more programs involving function calls and helps efficient implementation of Pointer Logic rules;

2. We extend Pointer Logic with limited pointer arithmetic to verify the properties such as absence of array-out-of-bound errors, absence of null pointers involved in pointer arithmetic etc., besides the common guarantees of memory safety;

3. To demonstrate that Pointer Logic is a useful approach to verification, we implemented plcc(v2.0) to automatically verify a range of non-trivial pointer programs, including basic operations on lists, trees, circular doubly-linked lists, dynamic arrays. A bright feature of plcc(v2.0) is that it can generate human readable proof outlines when the verification is successful.

The rest of the paper is organized as follows. Section 2 defines the PointerC language. Section 3 introduces Pointer Logic briefly. Section 4 presents the modular reasoning in Pointer Logic. Section 5 extends Pointer Logic with pointer arithmetic. Section 6 shows the experimental results. Section 7 presents the related work and Section 8 concludes our work.

2. The PointerC language

PointerC is a C-like imperative language which excludes the address-of operation (&). The syntax is given in Figure 1. The notation ς denotes a sequence of ς’s. Note that we extend the type with ς[]* to support dynamic array declarations and add a system call calloc. Currently we only allow pointer arithmetic on dynamic arrays. Every successful call of calloc(t, n) will return a dynamic array of type t[]* with length n. Also malloc and free functions are defined as system calls and meet the basic requirements of safe programs. For example, every call to malloc always successfully returns and the objects allocated are not overlapped in the heap. The type system is deferred to [21].

3. The Pointer Logic

In this section, we briefly introduce Pointer Logic. The details are deferred to [7]. The basic idea is to represent memory states by means of sets of pointers. Every dynamically allocated object is denoted by a valid pointer set π in which the r-values of the pointers are the same while l-values are distinct. A pointer is valid if and only if it points to a dynamically allocated object. A set of π sets representing all the objects in the heap is denoted by Π. Besides, there are two special sets: an Ν set for null pointer set and a D set for dangling pointer set which are used for the purpose of catching memory errors such as null pointer dereferences and dangling pointer dereferences etc. As the pointers in the same π set, the pointers in Ν or D are also with distinct l-values. Note the representation captures the heap structure exactly, for every object is described by a set π and the pointers in these sets maintain the relationships between objects.

For example, in Figure 2, the representation of Π is

![Figure 2. An example of Π, Ν, and D.](image)

\{ {p, q}, {p->next}, {p->next->next->next, r} \}, Ν is \{ {r->next} \}, and D is \{ s \} (The cross in s represents meaningless locations and "" means null). In Π, q->next does not show up in set \{ p->next \} because q->next and p->next have the same l-value. In Pointer Logic, \{ p, q \} denotes object Oₐ, \{ p->next \} denotes object Oₐ, while \{ p->next->next->next, r \} denotes object Oₗ. As a result, the Π, Ν, and D sets capture the topological structure of the heap exactly, the information of which is useful for program verification.

3.1. The assertion language

In this section, we define the assertion language used for program annotation. The syntax is given in Figure 3. Not
all the sentences derived by this grammar can be assertions
here: (i) Pointer sets derived are operands of conjunction and
disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-
tive operator; (ii) The disjunction operators, but can not be operands of the nega-

Figure 3. The assertion language.

4.1. Objects and reachability

To make the reasoning more uniform, we introduce objects
and reachability in this section.

In Pointer Logic every dynamically allocated object $O$ is
represented by a set of pointers pointing to $O$. Here we
extend the concept about objects by assuming that every
pointer in $N$ or $D$ points to different virtual objects. This
makes sense because the following rules hold in Pointer
Logic:

\[
\{p_1, p_2, \ldots, p_n\}_N = \{p_1\}_N \land \{p_2\}_N \land \ldots \land \{p_n\}_N \quad (1)
\]

\[
\{p_1, p_2, \ldots, p_n\}_D = \{p_1\}_D \land \{p_2\}_D \land \ldots \land \{p_n\}_D \quad (2)
\]

Thus we can imagine that they are pointing to some virtual
objects in the heap.

DEFINITION 4.1 (Reachability) An object, represented
by a set $S$, either a $\pi$ set, or $\{x\}_N$, or $\{x\}_D$, is
reachable from pointer $p$, if and only if there exists pointer
$q \in S$ such that $\exists r. r \in \text{closure}(q) \land \text{prefix}(p, r)$. The
relationship of reachability is denoted by $\text{Reach}(p, S)$.

The two functions $\text{closure}$ and $\text{prefix}$ are defined in [7], in
which $\text{closure}(p)$ returns all the pointers that are with the
same l-value as $p$, and $\text{prefix}(p, r)$ decides whether pointer
$p$ is a prefix of $r$. Based on definition 4.1, we can define a
function to describe objects reachable from a set of pointers.
Let $S = \{p_1, \ldots, p_n\}$ be a set of pointers, we define:

\[
R(S) \triangleq \bigcup_{i=1}^{n} \Pi_{p_i} \land \bigcup_{i=1}^{n} \mathcal{N}_{p_i} \land \bigcup_{i=1}^{n} \mathcal{D}_{p_i} 
\]

where $\Pi_{p_i} \triangleq \{ \pi \mid \pi \in \Pi \land \text{Reach}(p_i, \pi) \}$; $\mathcal{N}_{p_i} \triangleq \{ q \mid q \in \mathcal{N} \land \exists r. r \in \text{closure}(q) \land \text{prefix}(p_i, r) \}$; $\mathcal{D}_{p_i} \triangleq \{ q \mid q \in \mathcal{D} \land \exists r. r \in \text{closure}(q) \land \text{prefix}(p_i, r) \}$. 

4.2. Inference rules

First, we concentrate on the assignment rules from [7].
Existing rules for a destructive update have to perform a
substitution operation on all the sets of $\Pi$, $\mathcal{N}$ and $\mathcal{D}$. Now
that we have the $R$ function, we only have to update part of
function calls associate the entire heap with each invoca-
tion, and the function body might be verified more than
once. However, a program often accesses part of the heap
instead of the whole heap. When we annotate a function, its
precondition only describes part of the heap which may be
modified by the function body. Thus modular treatment of
heaps for function call is a necessity. Furthermore, modular
reasoning helps efficient implementation of Pointer Logic
rules.
Moreover, highly efficient assembly code can be obtained by using pointer arithmetic. However, flexible pointer arithmetic might bring array-out-of-bound error when dereferencing a pointer pointing to some element of an array. There are cases when null pointers or dangling pointers are involved in pointer arithmetic, while it is difficult to detect via type checking. The goal of extending Pointer Logic with pointer arithmetic is to verify pointer program properties related to the correct use of dynamically allocated memory such as absence of null pointers or dangling pointers involved in pointer arithmetic, absence of array-out-of-bound errors, besides the common guarantees of absence of null dereferences, memory leaks etc. Here, we study the reasoning in Pointer Logic by allowing limited pointer arithmetic as a probe.

Since Pointer Logic collects pointer information which is about the pointers pointing to heap blocks, we only allow pointer arithmetic on pointers pointing to one-dimensional dynamic arrays which are allocated by calloc(T, n). Function calloc is defined as a system call where $T$ is the type of elements and $n$ is the length of the array. An example of using calloc and pointer arithmetic is shown in Figure 4.

$$T[] \ast q; \ T \ast p, \ast r;\ q=\text{calloc}(\ T, 10); \ p=q+5; \ r=p+3;$$

**Figure 4. An example for pointer arithmetic.**

In Pointer Logic, when $p \neq q$ (we denote by $\equiv$ syntactic equivalence), we use a triple $<p, q, \text{offset}>$ to denote pointers pointing to a dynamic array, where $p$ is the inner pointer with type $T_3$, $q$ is the base pointer with type $T []^*, \text{and} \ offset$ indicates the position in the dynamic array, i.e., $p=q+\text{offset}+\text{sizeof}(T)$. In this case, the triple expresses the fact that pointer $p$ points to position $\text{offset}$ in a dynamic array $q$. When $p \equiv q$, the triple $<p, q, \text{offset}>$ just means the length of the dynamic array $p$ is $\text{offset}$. Note that the triple we define records the information about pointers. For example, in Figure 4, after an assignment $p=q+5$, the triple for $p$ is $<p, q, 5>$; after another assignment $r=p+3$ the triple for $p$ is the same, while the triple for $r$ is $<r, q, 8>$.

In order to simplify the reasoning, we require that all pointers pointing to dynamic arrays be root variables, and that the elements of a dynamic array be of a simple type without pointer fields, otherwise the form of the pointer won’t be uniform and therefore will greatly complicate the reasoning. However, these constraints can be relieved by introducing more general and uniform representations of pointers and rewriting more universal Pointer Logic rules.

### 5. Pointer Logic with pointer arithmetic

The advantage of pointer arithmetic is its flexibility and convenience for the programming, such as accessing array elements using the pointer itself as a loop control variable. Moreover, highly efficient assembly code can be obtained by defining the rule for $ret = f(y_1, \ldots, y_n)$.

#### 5.1. Axioms and inference rules

In this section, we introduce the axioms and rules involving pointer arithmetic. In accordance with the rules in [7], we try to make the minimum changes by adding a new kind
of set $C$ (See Figure 3) which is made up of a set of triples describing pointers pointing to dynamic arrays. When two pointers point to non-dynamic-array structures, the rules are the same as in [7] since the program won’t modify any elements in $C$. As a result, the rules in [7] can be treated as a special case when $C$ is empty or $C$ stays the same. In essence, $C$ is a loose form describing pointers – every base pointer in $C$ is valid, every inner pointer is either valid or dangling, the state of which depends on the value of offset. If offset is within the scope of the corresponding array, then the pointer is valid, else it is dangling. Hence triples classify themselves, and there is no need to classify the triples in $C$ into more sets just as $\Pi, \mathcal{N}$ and $\mathcal{D}$ sets do. Note that inner pointers won’t point to elsewhere, i.e., they won’t appear in $\Pi, \mathcal{N}$ or $\mathcal{D}$. However, the pointers with dynamic array type must appear in II, $\mathcal{N}$ or $\mathcal{D}$, because a dynamic array as a whole can be viewed as an object in the heap.

To ease notation in the extended rules, we introduce some helper functions and shortcuts shown in Figure 5. Notation $x.eq$ defined in [7] returns the equivalent set

$$C \setminus p \triangleq \{ <p', q', e> \mid <p', q', e> \in C \land \exists q'' \in q'.eq \land (p' \land p' \in \text{closure}(p) \Rightarrow \text{prefix}(p', q'')) \}$$

$$C - p \triangleq \{ <p', q', e> \mid <p', q', e> \in C \land p' \notin \text{closure}(p) \}$$

$$C + <p, q, n> \triangleq C \cup \{ <p, q, n> \}$$

$$C - \{ p_1, \ldots, p_n \} \triangleq (\ldots (C - p_1) \ldots - p_n)$$

$$p <: \mathcal{C} \triangleq \exists p', q', e \in C : (p' \land p < p' < q' \land p < p'.eq)$$

$$p <: \mathcal{R} \triangleq \exists q \in \mathcal{R} \land q \notin \text{closure}(p)$$

$$\mathcal{R} + p \triangleq \mathcal{R} \cup \{ p \}$$

$$p <: \Pi \triangleq p.\text{eq} \in \Pi$$

$$\Pi + p \triangleq \Pi \cup \{ p \}$$

$$\text{base}(p) \triangleq q \text{ where } \exists e : <p, q, e> \in C$$

$$\text{index}(p) \triangleq e \text{ where } \exists q : <p, q, e> \in C$$

**Figure 5. Shortcuts and helper functions.**

pointer $x$ is in. $C \setminus p$ deals with substitutions for every base pointer $q'$ which is prefixed by an alias of $p$, with another pointer $q''$. $C - p$ just removes the triple describing pointer $p$. $p <: C$ means that $p$ is either an inner pointer or a base pointer. Meta variable $\mathcal{R}$ denotes a set of pointers.

Because of the constraints we mentioned above, the rules are simpler than we may have thought. The most important of all, all the rules in [7] can be reused. However, the introduction of $C$ requires more rules to deal with dynamic array assignment. We only highlight the differences.

1) Pointer $p$ and $q$ are pointing to non-dynamic-array structures:

$$p \notin C \land q \notin C \Rightarrow \frac{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \} \ p = q \{ \Pi' \land \mathcal{N}' \land \mathcal{D}' \land C\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (7)$$

2) Pointer $p$ and $q$ are of dynamic array type:

$$\frac{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \} \ p = q \{ \Pi' \land \mathcal{N}' \land \mathcal{D}' \land C\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (8)$$

$$\frac{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \} \ p = q \{ \Pi' \land \mathcal{N}' \land \mathcal{D}' \land C\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (9)$$

Rule (8) and (9) are analogous to rule (7) in that the modification of the II, $\mathcal{N}$ and $\mathcal{D}$ part is obtained through the rules in [7]. The no_leak function defined in [7] ensures no memory leaks can occur.

3) Pointer $q$ is of dynamic array type, and $p$ is of its elements’ type:

$$\frac{p \notin \Pi \land p <: C \land q <: \Pi \land q <: C \land \mathcal{N} \land \mathcal{D} \land C \ p = q + e \{ \Pi \land \mathcal{N} \land \mathcal{D} \land (C - p < p, q, e)\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (10)$$

$$\frac{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \} \ p = q + e \{ \Pi \land \mathcal{N} \land \mathcal{D} \land (C - p < p, q, e)\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (11)$$

The intermediate assertion $\Pi' \land \mathcal{N}' \land \mathcal{D}'$ is obtained through the corresponding rule in [7].

4) Pointer $p$ and $q$ are both of dynamic-array-element type for assignment $p = q + e$:

$$\frac{p \notin \Pi \land p <: C \land q <: C \land q \notin \Pi \land \mathcal{N} \land \mathcal{D} \land C \ p = q + e \{ \Pi \land \mathcal{N} \land \mathcal{D} \land (C - p < p, \text{base}(q), \text{index}(q) + e)\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (12)$$

$$\frac{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \} \ p = q + e \{ \Pi \land \mathcal{N} \land \mathcal{D} \land (C - p < p, \text{base}(q), \text{index}(q) + e)\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (13)$$

5) Pointer $p$ is of dynamic-array-element type:

$$\frac{p <: C \land \mathcal{N} \land \mathcal{D} \land C \ p = \text{NULL} \{ \Pi \land \mathcal{N} \land \mathcal{D} \land (C - p)\}}{\{ \Pi \land \mathcal{N} \land \mathcal{D} \land C \}} \quad (14)$$
The above rules for pointer assignment only concern about the modification of pointer sets. Often, the precondition is \( \Psi \) accompanied by assertion \( Q \) and some \( l\)-values in \( Q \) may contain pointer prefixes. Here we just give the corresponding rule for rule (12) and (13), and the rest are omitted for space limitations.

\[
\{ \Psi \land Q \} \ L = q \oplus e \{ \Psi' \land Q[r \leftarrow \ell p'/p] \} \quad (15)
\]

where

\[
p' \triangleq \begin{cases} \text{if} \ base(p) \equiv base(q) \ \text{then} \ q*(\text{index}(p)-\text{index}(q)) \\ \text{else if} \ p \equiv q \ \text{then} \ p-e \ \text{else} \ base(p)+\text{index}(p) \end{cases}
\]

and \( \Psi' \) is obtained through the corresponding rule (12) or (13). Note that \( Q[r \leftarrow \ell p'/p] \) means that for every pointer \( r \) in \( Q \), if \( r \) has a prefix that has the same \( l \)-value as \( p \), then we replace the prefix with \( p' \).

7) The rules for \( \text{calloc} \) and \( \text{free} \) are given below:

\[
\begin{align*}
\{ \Pi \land \mathcal{N} \land D \} & \ P = \text{NULL} \ \{ \Pi' \land \mathcal{N}' \land D' \} \\
\{ \Pi \land \mathcal{N} \land D \land C \} & \ P = \text{calloc}(T,n) \\
\{ (\Pi' + p) \land (\mathcal{N}' - p) \land D' \land (C,p + <p,p,n>) \}
\end{align*}
\]

\[
\begin{align*}
p <: \Pi \land p <: C & \land \\
\{ \Pi \land \mathcal{N} \land D \} & \text{free}(p) \ \{ \Pi' \land \mathcal{N}' \land D' \} \\
\{ \Pi \land \mathcal{N} \land D \land C \} & \text{free}(p) \ \{ \Pi' \land \mathcal{N}' \land D' \land (C,p + <p,p,n>) \land \langle C - \{ p, p_1, \ldots, p_n \} \rangle \}
\end{align*}
\]

Note that in rule (16), pointer \( p \) must appear in \( \Pi, \mathcal{N} \) or \( D \), because \( p \) must be of dynamic array type. Thus it is safe to use the rules in [7] to obtain an intermediate state \( \Pi' \land \mathcal{N}' \land D' \). Adding \( <p,p,n> \) to \( C \) just describes the length of the dynamic array \( p \) points to is \( n \), which is to be used for array-out-of-bound check. The rule for \( \text{free} \) is based on the following assumptions: (i) the dynamic array is pointed to by \( p_1, \ldots, p_n \); (ii) \( p \) is of dynamic array type; (iii) \( p_1, \ldots, p_n \) are of its elements’ type.

5.2. Case study

In this section, we show how Pointer Logic extended with pointer arithmetic can be used in verification by illustrating an example with its proof outline shown in Figure 6. Note that dereferencing only occurs in if statement, and we guarantee that the dereferencing is safe – where \( p \) points to is within the length of the array. From \( <p,a,i> \) we know \( p \) points to the \( i \)-th position in the array, and \( i \geq 0 \land n \geq 1 \land i < n \) ensures that \( i \geq 0 \land i < n \) holds.

6. Experimental evaluation

Our approach has been efficiently implemented in a tool called plcc, and now its newest version is 2.0. Compared to the previous version of plcc(v1.5) (see [6, 7]), plcc(v2.0) has the following advantages: (i) plcc(v2.0) is fully automated, while the verification conditions generated by plcc(v1.5) need proving manually in COQ [8]; (ii) With support for modular reasoning and pointer arithmetic, plcc(v2.0) can verify a range of programs while plcc(v1.5) can only handle several simple programs; (iii) plcc(v2.0) automatically generates a human readable proof outline file for each program when the verification is successful. The proof outline file is of great use for us to debug programs. plcc(v2.0) not only verifies the basic safety properties of correct programs, but also detects errors such as possible memory leaks, null dereferences, dangling pointer dereferences, trying to free null pointers or dangling pointers. Thus plcc(v2.0) can be used as a tool for statically checking errors.

We have assessed our calculus on a number of pointer programs, as shown in Table 1. In all examples verified by plcc, we are ensured that no memory errors could occur. All measurements were performed on a machine using a 1.73GHz Intel PentiumM CPU with 1GB memory. We have verified commonly used operations on singly-linked lists, circular doubly-linked lists, trees, dynamic arrays. The verification time of each program is less than 10 seconds, which is insignificant compared to the time required to design an algorithm and annotate the code. The source code and all the examples’ proof outline files are available in reference [21].

<table>
<thead>
<tr>
<th>Test case</th>
<th>Code size (Byte)</th>
<th>Proof outline size (KB)</th>
<th>Time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>listReverse</td>
<td>405</td>
<td>10.9</td>
<td>0.062</td>
</tr>
<tr>
<td>listCreate</td>
<td>494</td>
<td>12.6</td>
<td>0.110</td>
</tr>
<tr>
<td>listDestroy</td>
<td>389</td>
<td>6.03</td>
<td>0.031</td>
</tr>
<tr>
<td>listGetElement</td>
<td>839</td>
<td>17.6</td>
<td>0.281</td>
</tr>
<tr>
<td>listInsertNth</td>
<td>891</td>
<td>33.6</td>
<td>0.547</td>
</tr>
<tr>
<td>listDeleteNth</td>
<td>843</td>
<td>30.5</td>
<td>0.656</td>
</tr>
<tr>
<td>listZip</td>
<td>1,051</td>
<td>70.9</td>
<td>0.203</td>
</tr>
<tr>
<td>listRotate</td>
<td>564</td>
<td>12.5</td>
<td>0.125</td>
</tr>
<tr>
<td>listConcat</td>
<td>584</td>
<td>17.9</td>
<td>0.141</td>
</tr>
<tr>
<td>dlistInsertNth</td>
<td>1,085</td>
<td>59.1</td>
<td>2.390</td>
</tr>
<tr>
<td>dlistDeleteNth</td>
<td>1,061</td>
<td>47.1</td>
<td>2.812</td>
</tr>
<tr>
<td>treeRightRotate</td>
<td>531</td>
<td>8.55</td>
<td>0.031</td>
</tr>
<tr>
<td>treeLeftRotate</td>
<td>531</td>
<td>8.55</td>
<td>0.031</td>
</tr>
<tr>
<td>treeDeleteNode</td>
<td>1,502</td>
<td>56.6</td>
<td>0.406</td>
</tr>
<tr>
<td>treeTraverse</td>
<td>325</td>
<td>4.28</td>
<td>0.031</td>
</tr>
<tr>
<td>treeCopy</td>
<td>493</td>
<td>13.3</td>
<td>0.047</td>
</tr>
<tr>
<td>treeDispose</td>
<td>316</td>
<td>5.85</td>
<td>0.016</td>
</tr>
<tr>
<td>maxMinValue</td>
<td>489</td>
<td>15.9</td>
<td>0.062</td>
</tr>
<tr>
<td>printDArray</td>
<td>366</td>
<td>10.0</td>
<td>0.047</td>
</tr>
</tbody>
</table>

Table 1. Experimental results.
int max, min;
void max_min_value(int a, int n) {
    int *p, *end;
    {a} ∧ <a, a, n> ∧ n ≥ 1} /* — precondition */
    void max_min_value(int a, int n) {
        int *p, *end;
        {a} ∧ <p, a, i> ∧ <end, a, n> ∧ <a, a, n> ∧ i < n ∧ i ≥ 0 ∧ n ≥ 1}
    } if (*p > max) { max = *p; } else if (*p < min) { min = *p; }
    } p = p + 1;
    } (p-1) > L0 ∧ max = *(p-1) ∨ *(p-1) ≤ max ∧ *(p-1) < L0 ∧ min = *(p-1) ∨ *(p-1) > min ∧ max ≥ *(p-1))}}
    } {a} ∧ <a, a, n> ∧ a ∧ n ≥ 1}
    return;
    } {a} ∧ <a, a, n> ∧ n ≥ 1} /* — postcondition */
Figure 6. Maximum and minimum value of a dynamic array.

7. Related work

Programming with pointers is difficult and risky. This has motivated a huge body of work concerned with analyzing pointer programs and verifying their properties. The most common way is to use Hoare logic to reason about pointer programs, e.g., [4, 13]. However, it’s difficult for the traditional Hoare approach to be automated. Besides, there are various extensions to Hoare logic for pointer verification, among which the most novel idea is separation logic. Separation logic [10, 17] is an extension of Hoare logic to reason about pointer structures through separating conjunction of domain disjointness. Recent work towards automation includes [2, 11]. In [2], an experimental tool called SMALLFOOT is implemented based on symbolic execution with separation logic [3]. It supports annotations for concurrency which is out of the scope of our approach, but lacks support for reasoning about pointer aliasing when positions are involved. In some circumstances, SMALLFOOT cannot verify the program using the rolling and unrolling technique alone, thus it uses a collection of inductive hypotheses, which means extra work and might be an obstacle for automatic checking – different data structures may need different hypotheses to help with the proof. In [11], a technique known as rippling is used for automatic assertion refinement, but yet there is no experimental evaluation.

In pointer program verification, the closest approach to ours is the one advocated by Jonkers [12]. There, the memory state is made of the set of all access paths in the data structures together with an equivalence relation (aliasing) on them. It had been further studied by Deutsch [9] to develop a may-alias algorithm. Recent publications include the work by Venet [20], Bozga et al. [5] and Rinetzky et al. [18]. Venet follows the earlier work of [12, 9], and proposes an analysis based on abstract interpretation that discovers potential sharing relationships among the data structures. Bozga et al. develop a weakest precondition calculus (an alias logic) for Jonkers’ storeless model with a Hoare-like proof system. Rinetzky et al. focus on local reasoning on Jonkers’ storeless model – an interprocedural analysis is described where objects are treated specially when they separate the “local heap” that can be mutated by a procedure from the rest of heap. However, these works based on Jonkers’ model suffer from the fact that their representation of memory states is redundant and costly, which can be a great obstacle to program verification. On the other hand, Pointer Logic not only enjoys most of the merits of being a storeless semantic approach, but also relieves its limitations and thus furthers the practical use of storeless approach.

In addition, shape analysis is also used for pointer program verification. PALE (Pointer Assertion Logic Engine) [14] is an automatic verification tool which encodes programs in Pointer Assertion Logic (PAL) – an extension of second order monadic logic on graph types which are tree-
shaped data structures with extra pointers. In PAL programs are restricted to updating only the underlying tree structure, therefore PAL is more applicable to programs manipulating graph types than to unrestricted imperative programs. In Pointer Logic, this is not the problem because our approach is based on sets of access paths describing the heap structure. Moreover, it is natural to adapt our approach for alias analysis, which seems to be an advantage over PAL.

TVLA (Three Valued Logic Analyzer) [19] is based on three valued logic to automatically abstract memory configurations. It is more automatic than ours in a sense that TVLA analyzes programs with only pre- and post-conditions, while our approach often requires the user to provide loop invariants. But still in TVLA the user may be required to provide some instrumentation predicates. Furthermore, because TVLA performs fixpoint iterations on abstract descriptions of the store, our approach using invariants is faster than TVLA.

8. Conclusion

This paper presents an extension of Pointer Logic for pointer program verification. First, we provide a method to deal with modular reasoning by introducing reachability to split program states. Then we extend Pointer Logic rules when limited pointer arithmetic is allowed in PointerC. Finally, we implement a tool – plcc (v2.0) to automatically verify a number of programs, including basic operations on lists, trees, circular doubly-linked lists. For the future, we are planning to apply our technique on compile-time garbage collection in Java. Furthermore, as the current Pointer Logic rules lack the ability to relate two states before and after a function call, the work to extend Pointer Logic with stamps is undergoing.

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